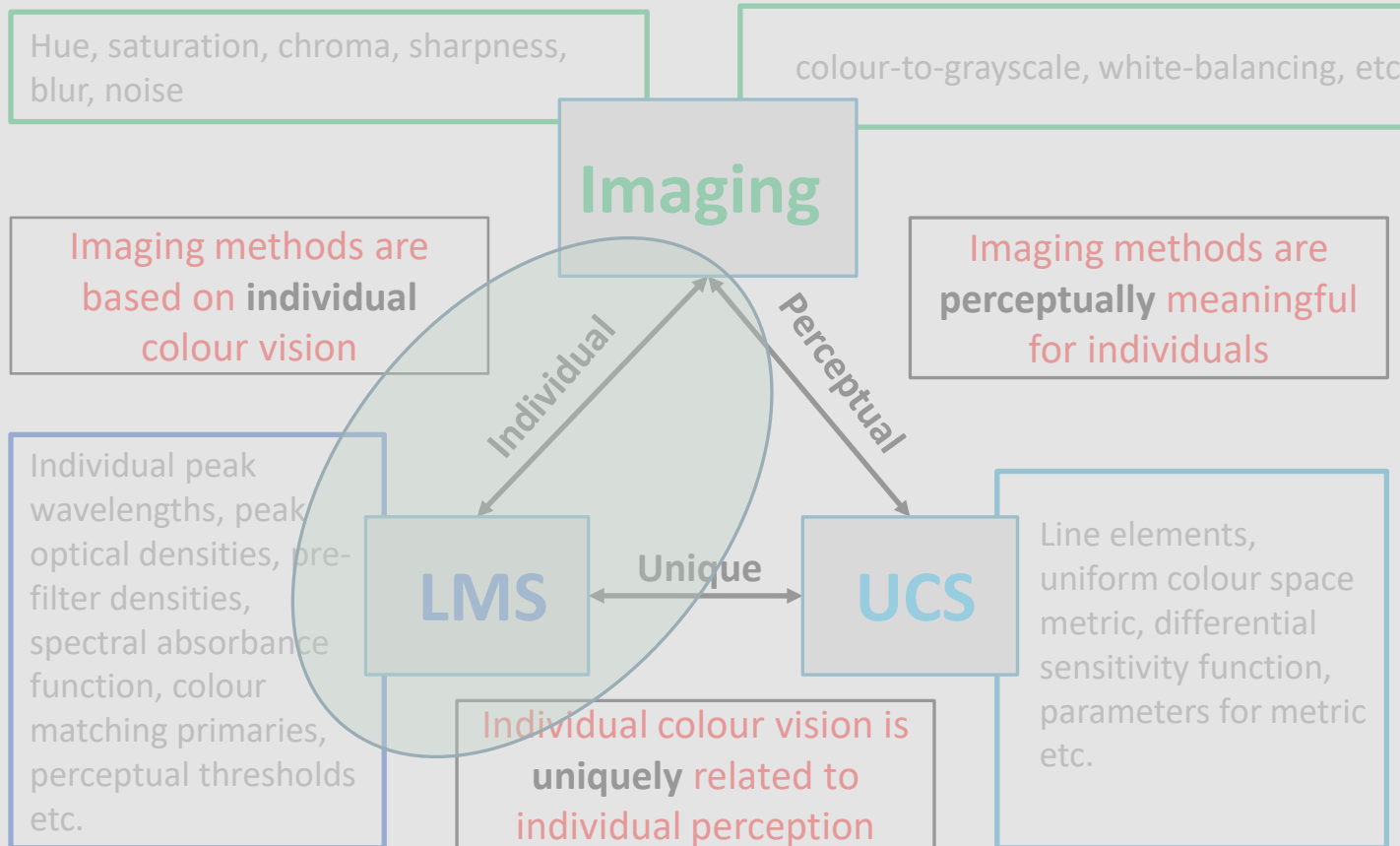


Measuring individual differences in colour-matching functions

LUVIN M RAGOO



- **Individual Colour Vision based Image Optimisation**
- Norwegian Research Council Funded (IKPLUSS), 2020-2024
- NTNU, Gjøvik, Norway
- Project Manager: Prof. **Ivar Farup**, Dept. Comp. Sc., NTNU
- Post Doc: MME(DTU, DK), phd(UEA, UK), **Casper Find Andersen**
- Phd stud.: MSc. (UEF, FI), **Luvín Ragoo**, Dept. Comp. Sc., NTNU
- Partner 1: Prof. **Graham D. Finlayson**, UEA, Norwich, UK
- Partner 2: Prof. **Edoardo Provenzi**, Univ. of Bordeaux, Bordeaux, France
- Partner 3: Assoc. Prof **Jan Henrik Wold**, Univ. College of S-East Norway, NTNU(currently)
- Lab assist: Assoc. Prof. **Peter Nussbaum**, Dept. Comp. Sc., NTNU

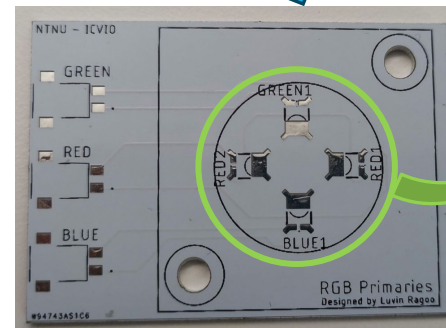
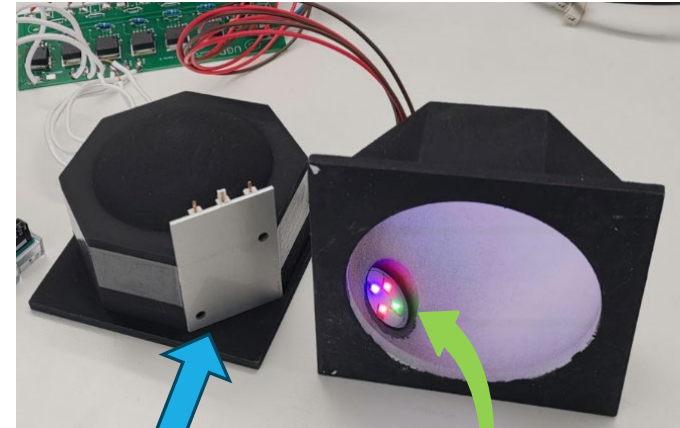
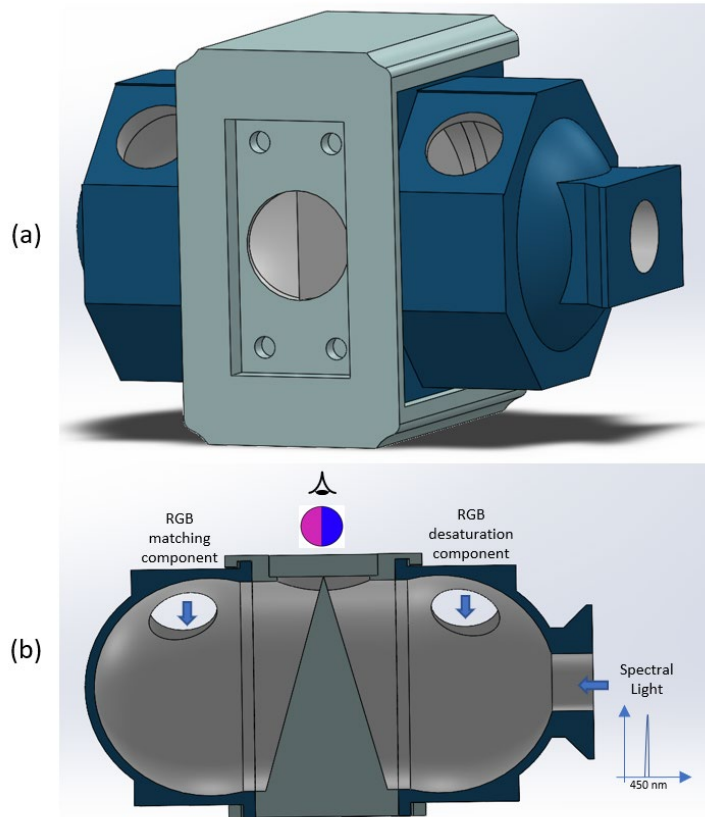


Aims

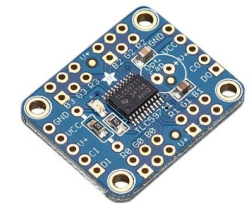
1. Develop a relatively simple experimental setup for measuring colour-matching functions.
2. Attempt to characterise observer metamerism in terms of their individual observer CMFs.
3. Estimation methods to streamline the process.

Colorimeter Design

First iteration



RGB LED Light Engine

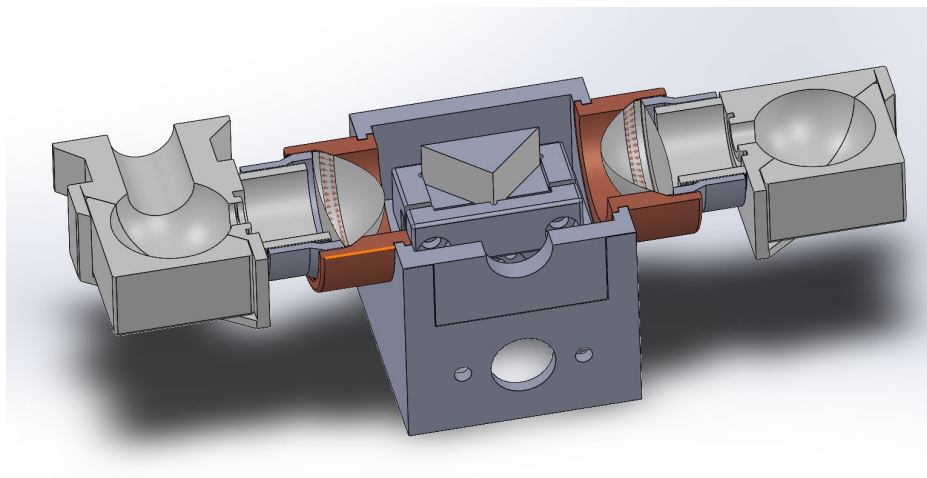
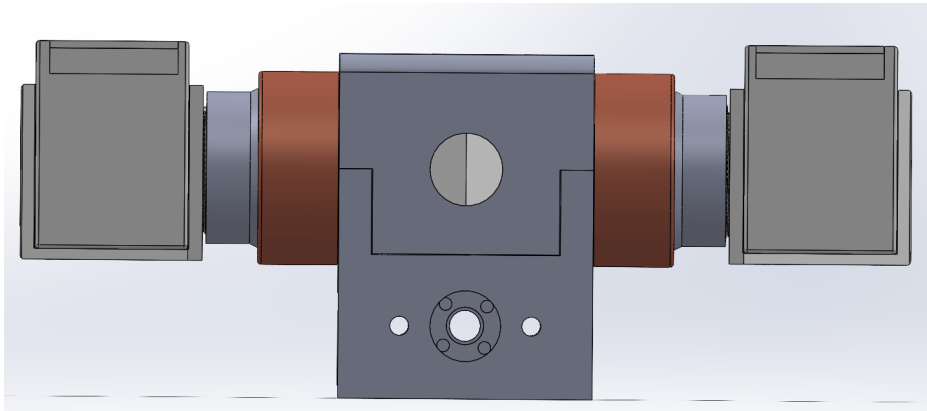


12-channel 16-bit PWM LED driver

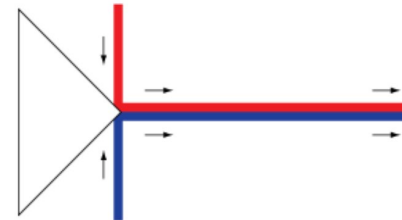
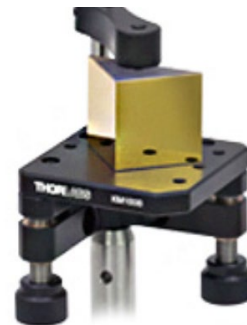
Rago, Luvin Munish, and Ivar Farup. "A Simple and Cost Effective Colorimeter for Characterising Observer Variability in Colour Matching Experiments." *London Imaging Meeting*. Vol. 4. Society for Imaging Science and Technology, 2023.

Colorimeter Design

Current iteration



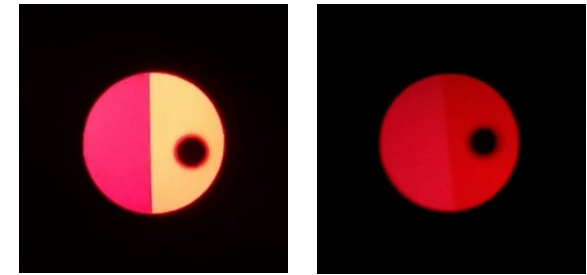
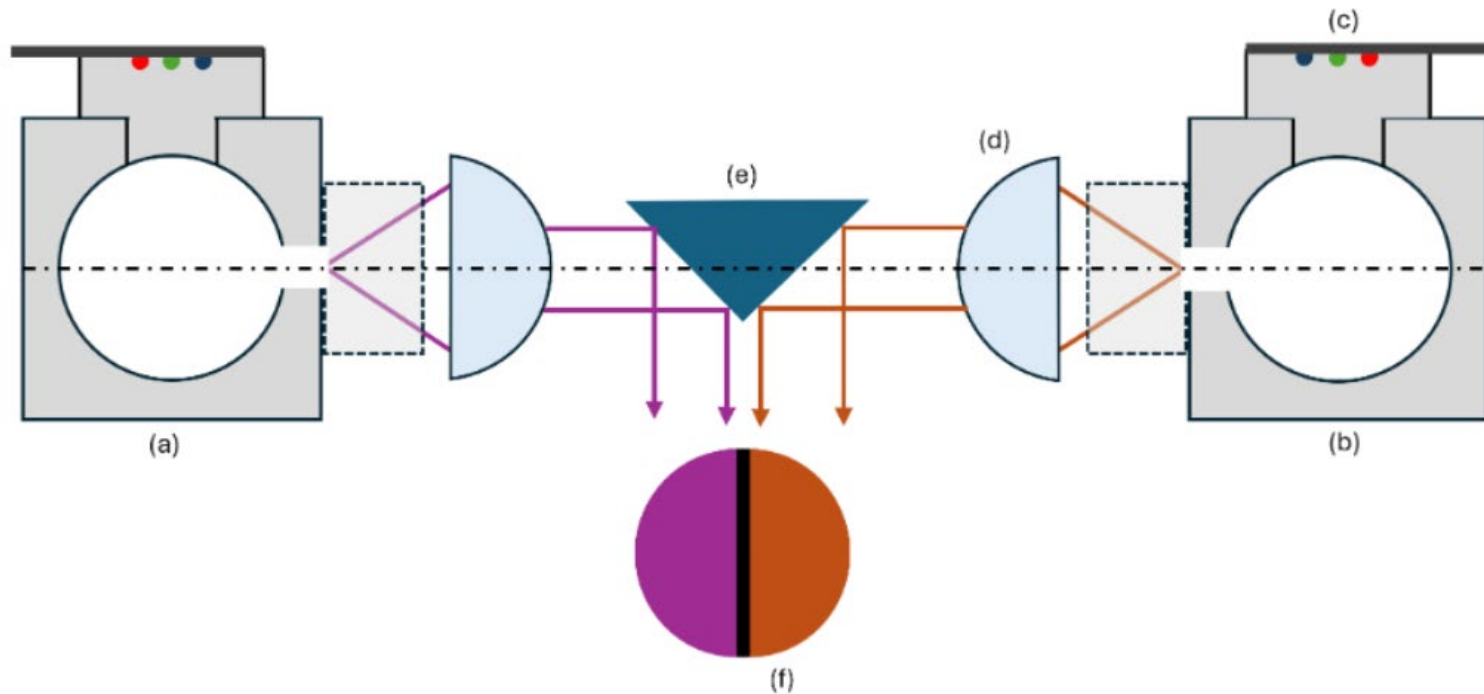
- Reduced the size of the integrating spheres to increase their efficiency.
- Adding collimating lenses to make the field more directional
- Knife-edge mirror to create a sharp bipartite field
- Lenses' positions adjustable such that light exiting the integrating spheres are right at the focal length → parallel rays incidenting on mirror → homogeneous bipartite field



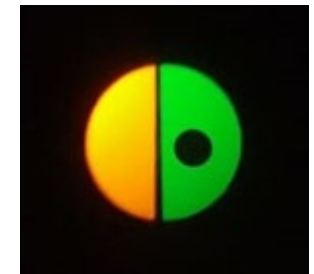
Ragoo, Luvin, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

Colorimeter Design

Current iteration



No gap



with gap

Fig. 1. Schematic diagram of the colorimeter. (a) Integrating chamber for the test field, it has two inputs (not shown on the diagram), the near-monochromatic test stimuli and the LED light engine. (b) The integrating chamber for the match field has only one input for the LED light engine. (c) LED light engine. (d) Aspheric condenser lens. (e) Knife-edge right-angle prism mirror. (f) Resulting bipartite field with adjustable gap width.

Ragoo, Luvin, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

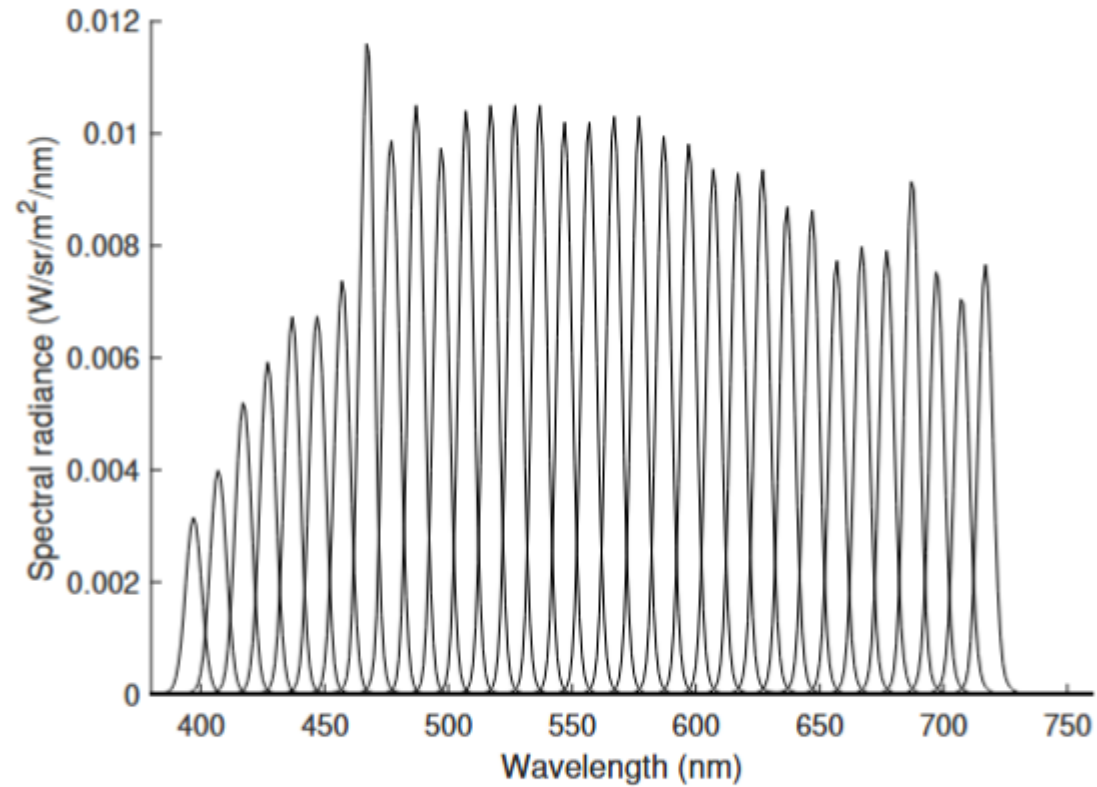


Figure 4. SPDs of the test lights

Ragoo, Luvín, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

Colorimeter Design

Characterisation : RGB LED lights

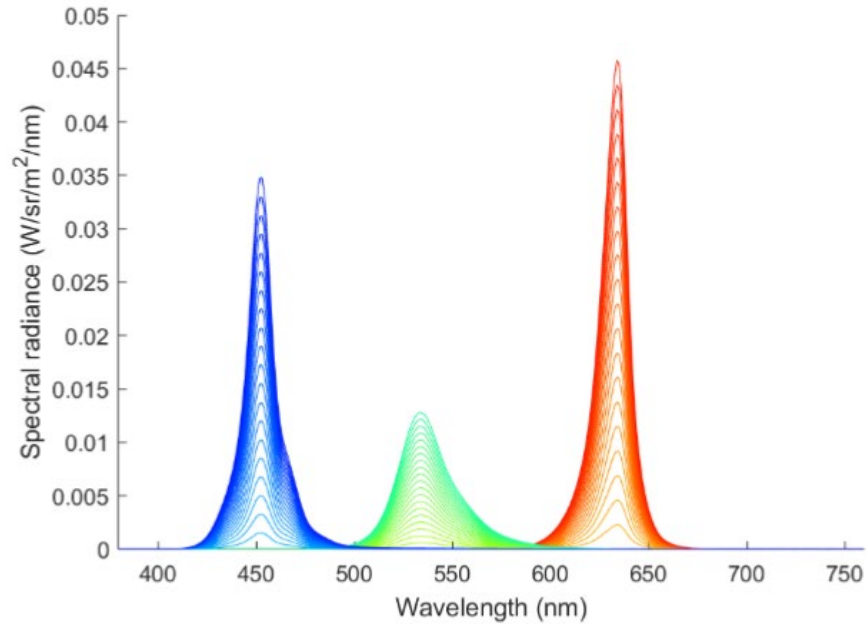


Figure 5. SPDs of the RGB LED lights at every 5 % intensity interval

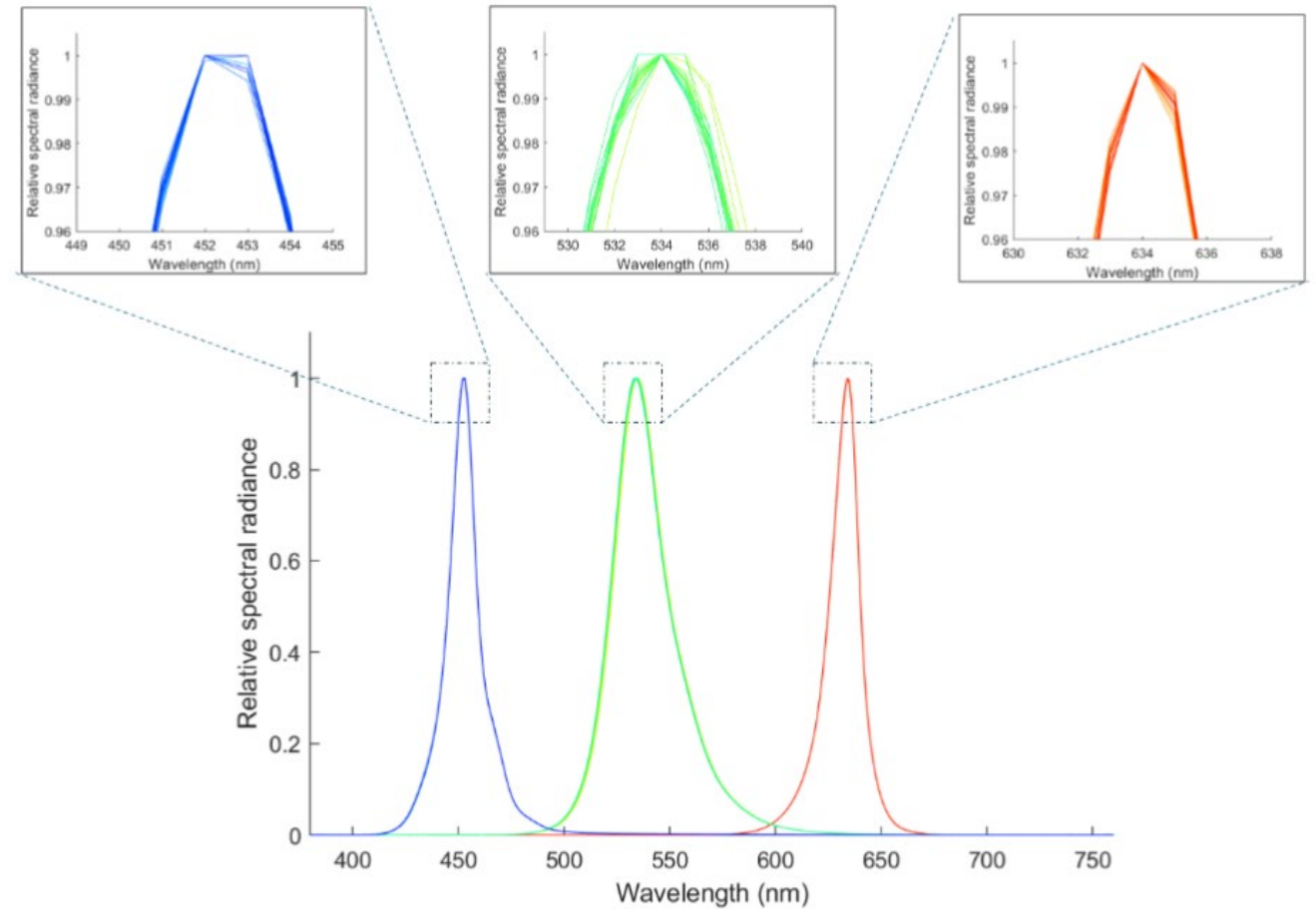


Figure 6. Relative SPDs of the RGB LED lights (normalisation to peak value of 1)

Ragoo, Luvin, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

Colorimeter Design

Characterisation : R, G, B reference stimuli

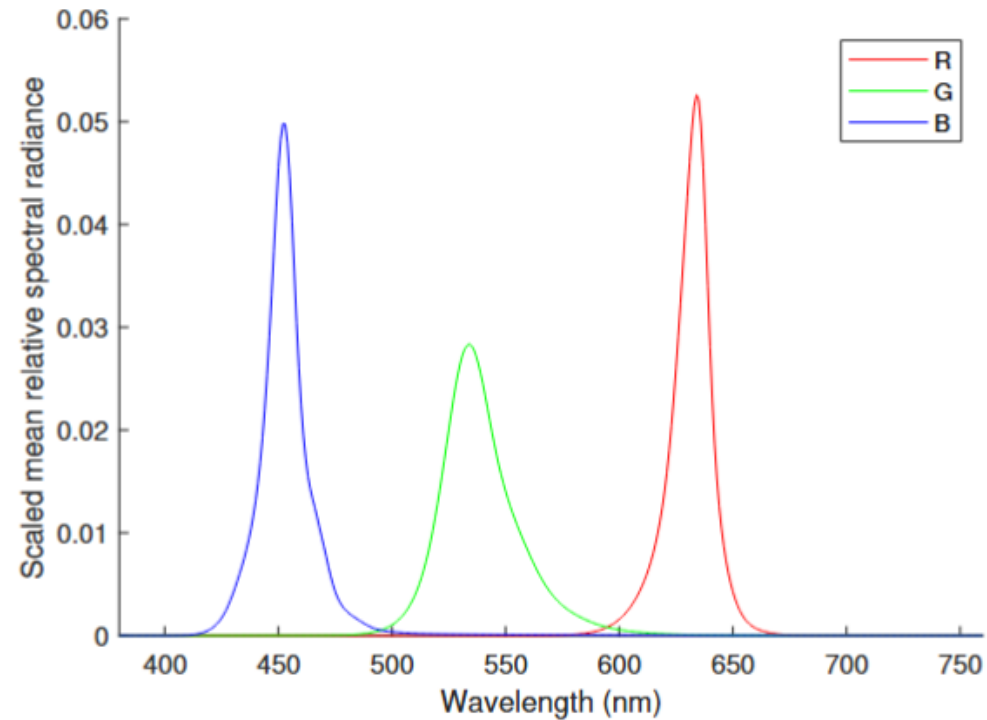
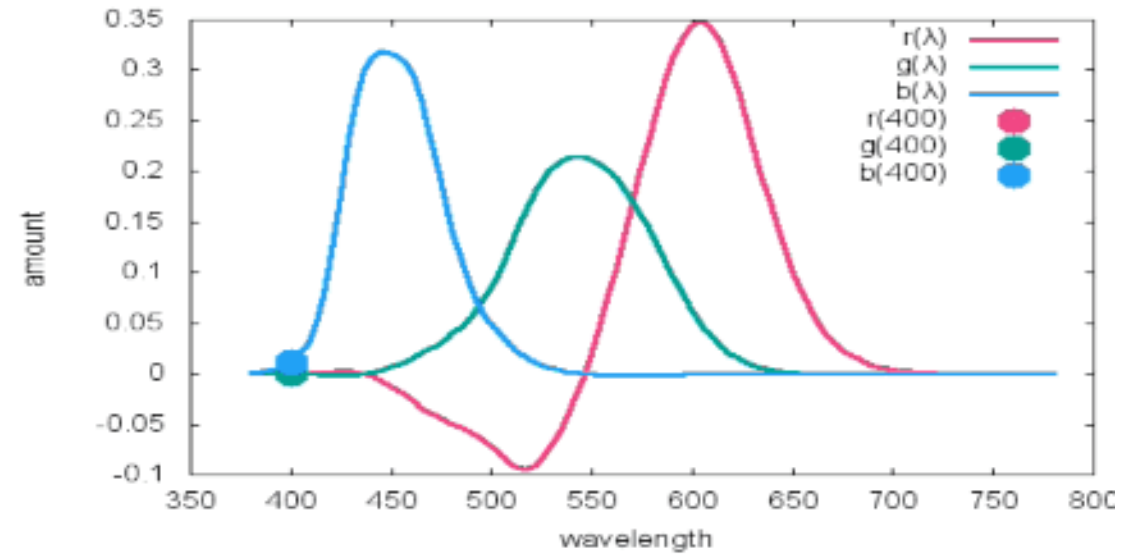
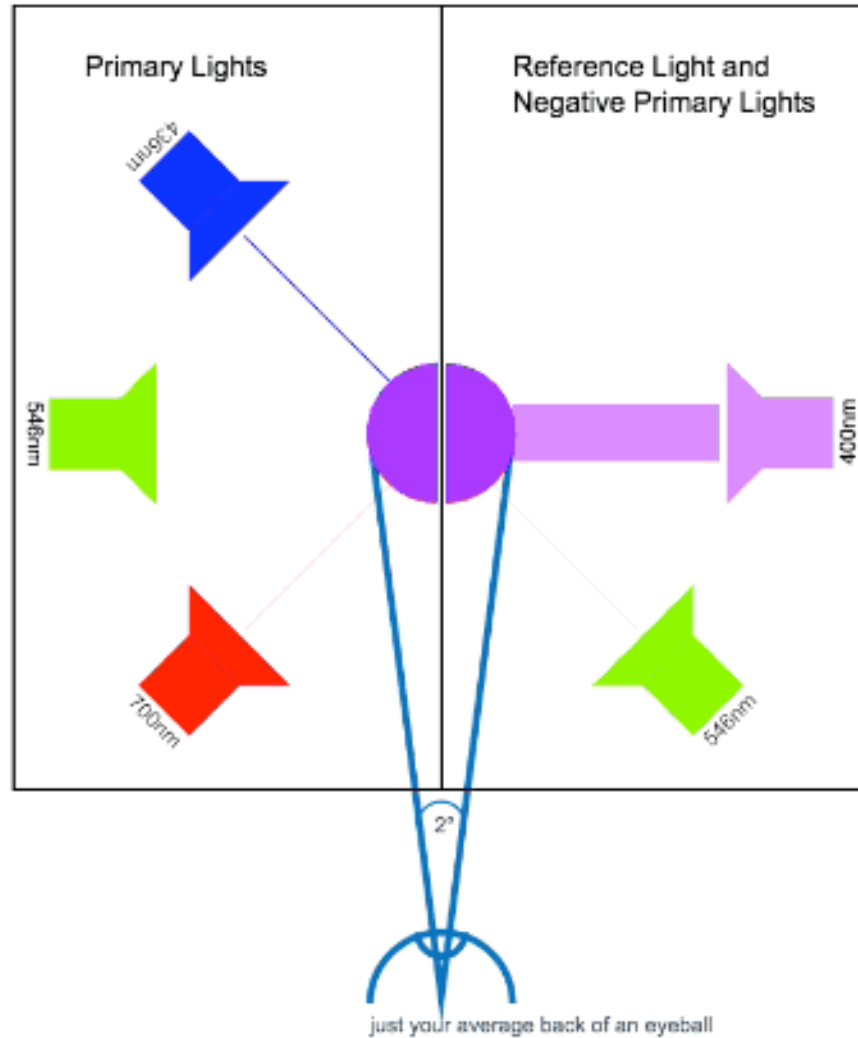


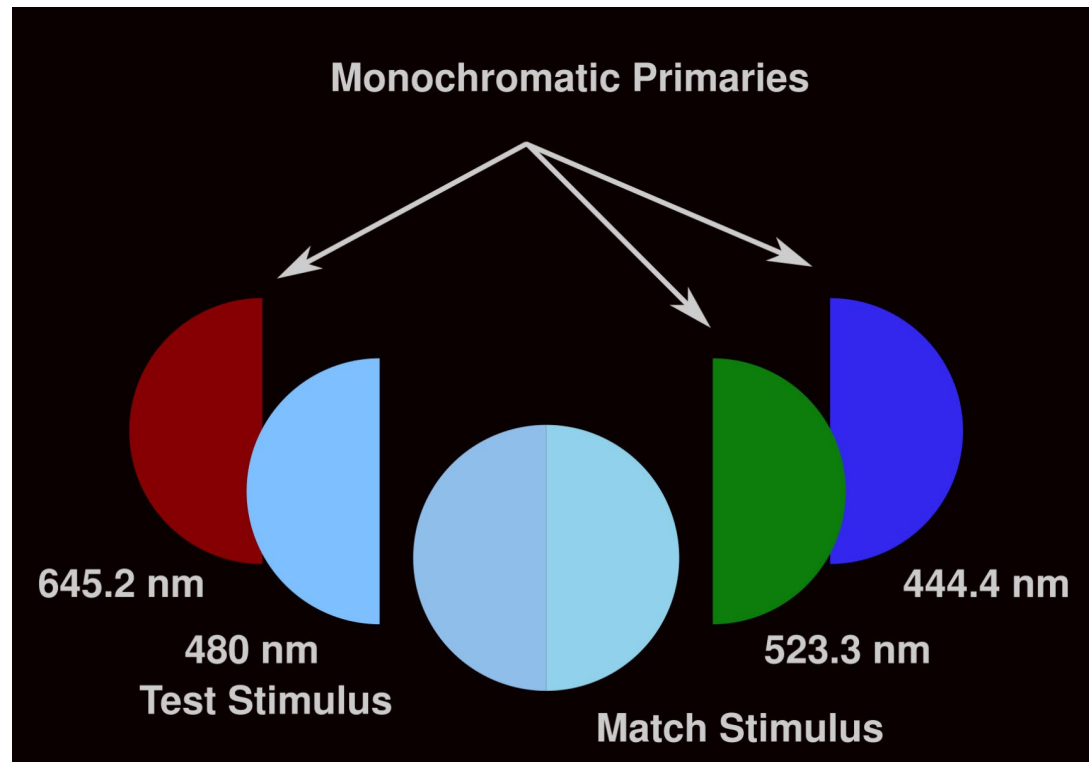
Figure 7. Scaled mean relative SPDs of the RGB LED lights, the scaling making their integrals (i.e. sums of their values at the sampling wavelengths of the spectroradiometer) all equal to 1 (The SPDs define the reference colour stimuli, **R**, **G**, and **B**.)

Ragoo, Luvín, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

Experiment Method

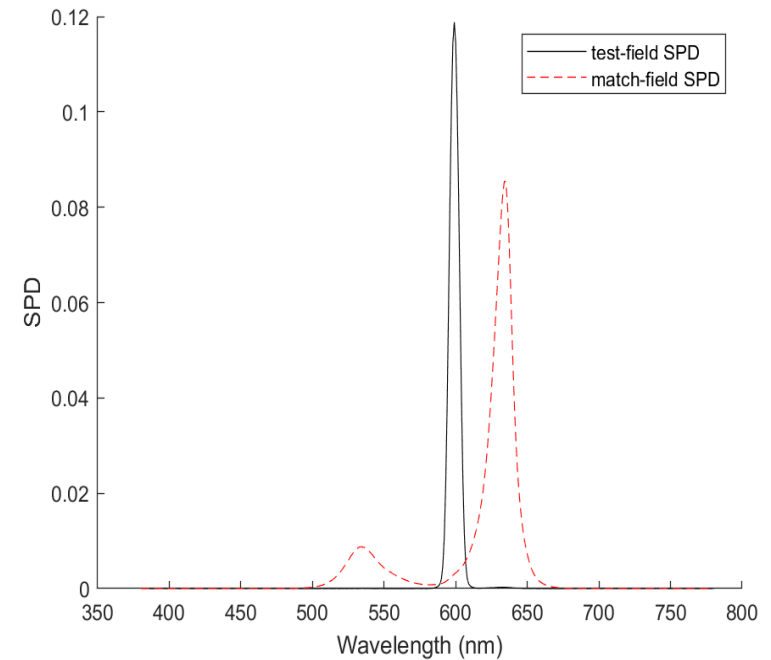


Reference : [A Beginner's Guide to \(CIE\) Colorimetry | by Chandler Abraham | Color and Imaging | Medium](#)



By Maneesh - Own work, CC BY-SA 4.0,
<https://commons.wikimedia.org/w/index.php?curid=105220816>

For example, for a test light of peak wavelength, 600 nm :



Experiment

Computing colour-matching coefficients

$$\mathbf{A}_{\lambda_i} = \begin{bmatrix} \mathbf{R} & \mathbf{G} & \mathbf{B} & \bar{\mathbf{S}}_{\lambda_i} \end{bmatrix} \quad \mathbf{A}_{\lambda_i} \mathbf{x}_{\lambda_i} = \mathbf{b}_{\lambda_i}$$

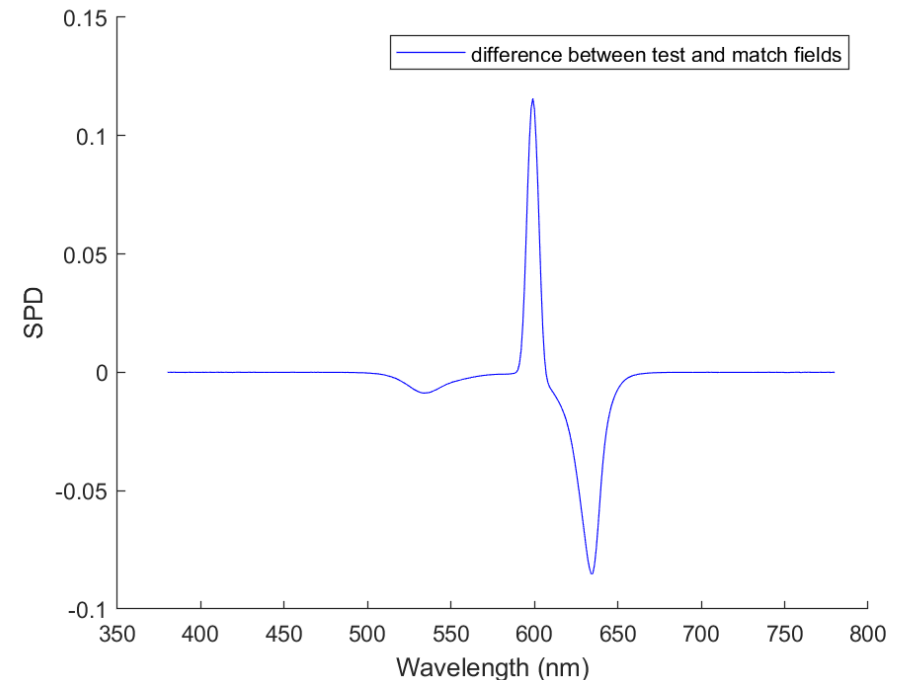
$$\mathbf{b}_{\lambda_i} = \bar{\mathbf{T}}_{\lambda_i} - \bar{\mathbf{M}}_{\lambda_i}$$

\mathbf{R} , \mathbf{G} , \mathbf{B} and \mathbf{S}_{λ_i} are 401 by 1 vectors representing the spectral power distribution of the Red, Green, Blue primaries and the spectral light at peak wavelength λ_i

\mathbf{b}_{λ_i} is a 401 by 1 vector representing the difference between the match and test field.

Finally, the coefficients for the primaries that would match a test stimulus with peak wavelength λ_i , can be obtained:

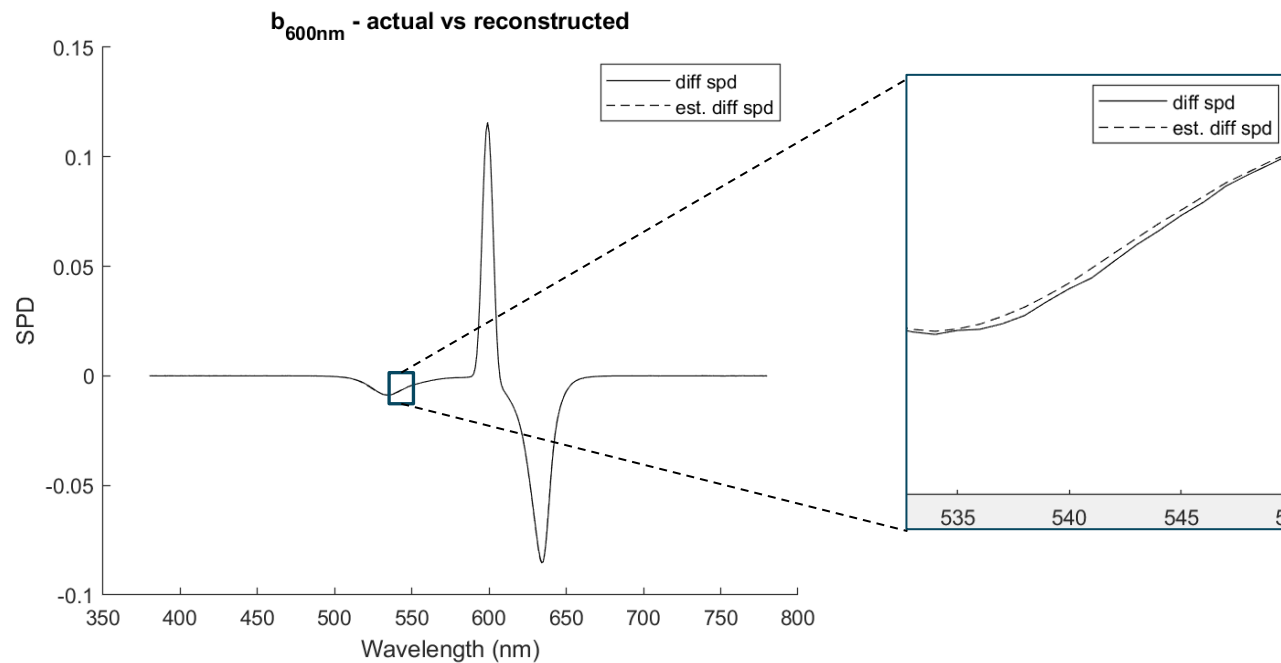
$$\mathbf{x}_{\lambda_i} = (\mathbf{A}_{\lambda_i}^T \mathbf{A}_{\lambda_i})^{-1} \mathbf{A}_{\lambda_i}^T \mathbf{b}_{\lambda_i}$$



Assessing estimation accuracy :

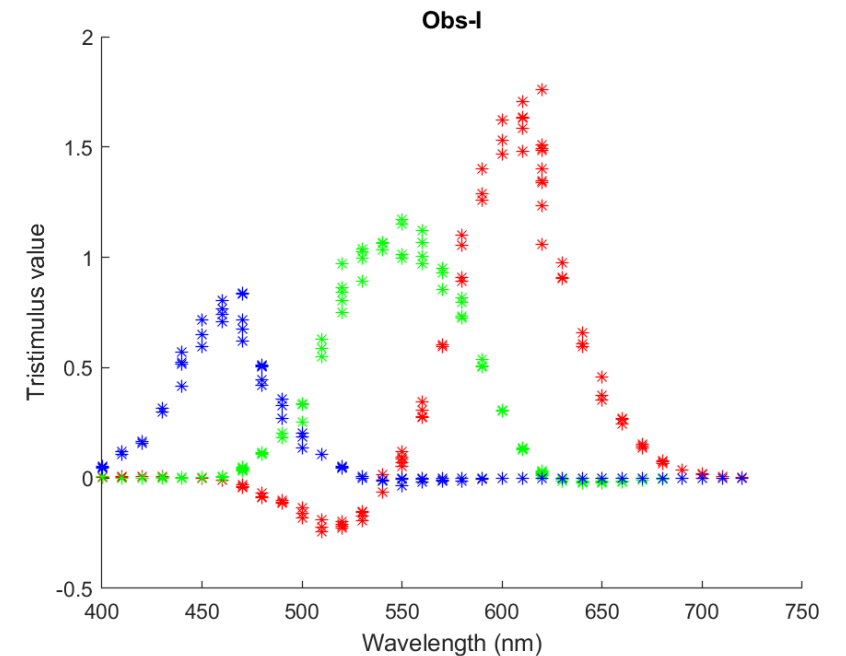
$$\text{PSNR}_{\mathbf{A}\mathbf{x},\lambda_i} = 20 \log_{10} \left(\frac{\max(\mathbf{b}_{\lambda_i})}{\text{rmse}(\mathbf{A}_{\lambda_i}\mathbf{x}_{\lambda_i}, \mathbf{b}_{\lambda_i})} \right)$$

(Gives a measure of the stability of the system)



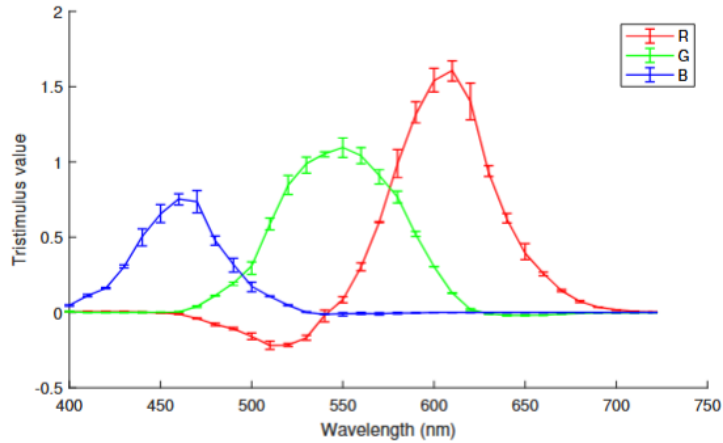
Assessing observer's matching uncertainty :

$$\text{PSNR}_{\mathbf{b},\lambda_i} = 20 \log_{10} \left(\frac{\max(\bar{\mathbf{b}}_{\lambda_i})}{\text{rmse}(\mathbf{b}_{\lambda_i}, \bar{\mathbf{b}}_{\lambda_i})} \right)$$

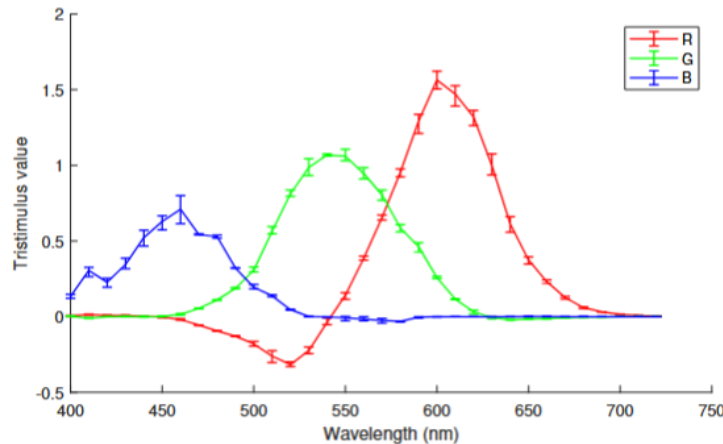


Results

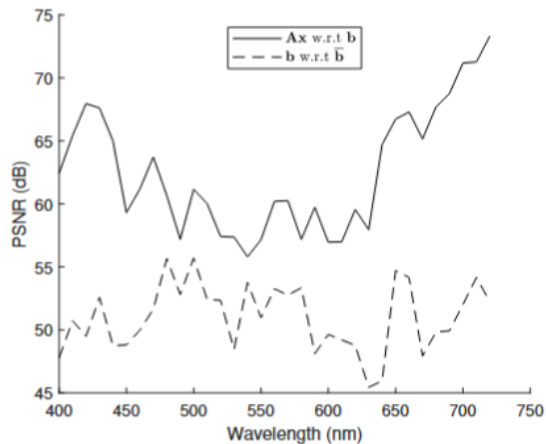
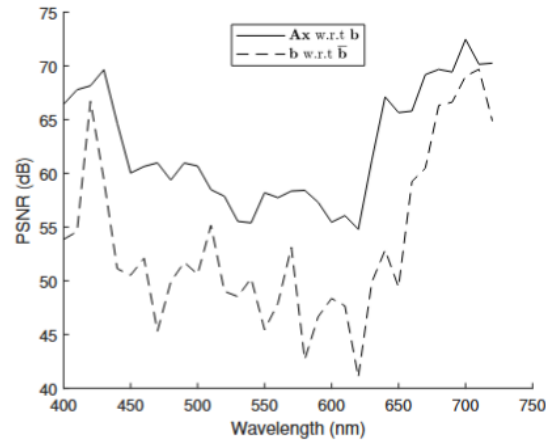
Individual Observer CMFs



Observer I



Observer T



CMF plots (on the left) :

- Mean CMFs are obtained from the average of the computed colour-matching coefficients, plotted at each test wavelength.
- Error bars represent the **95% confidence intervals** of the mean colour-matching coefficients (obtained by bootstrapping).

PSNR curves (on the right) :

- Solid curves show the **quality of estimation of colour-matching coefficients** at each test wavelength.
- Dashed curves show the **observers matching uncertainty** at each test wavelength.

Rago, Luvin, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

Results

Individual Observer CMFs

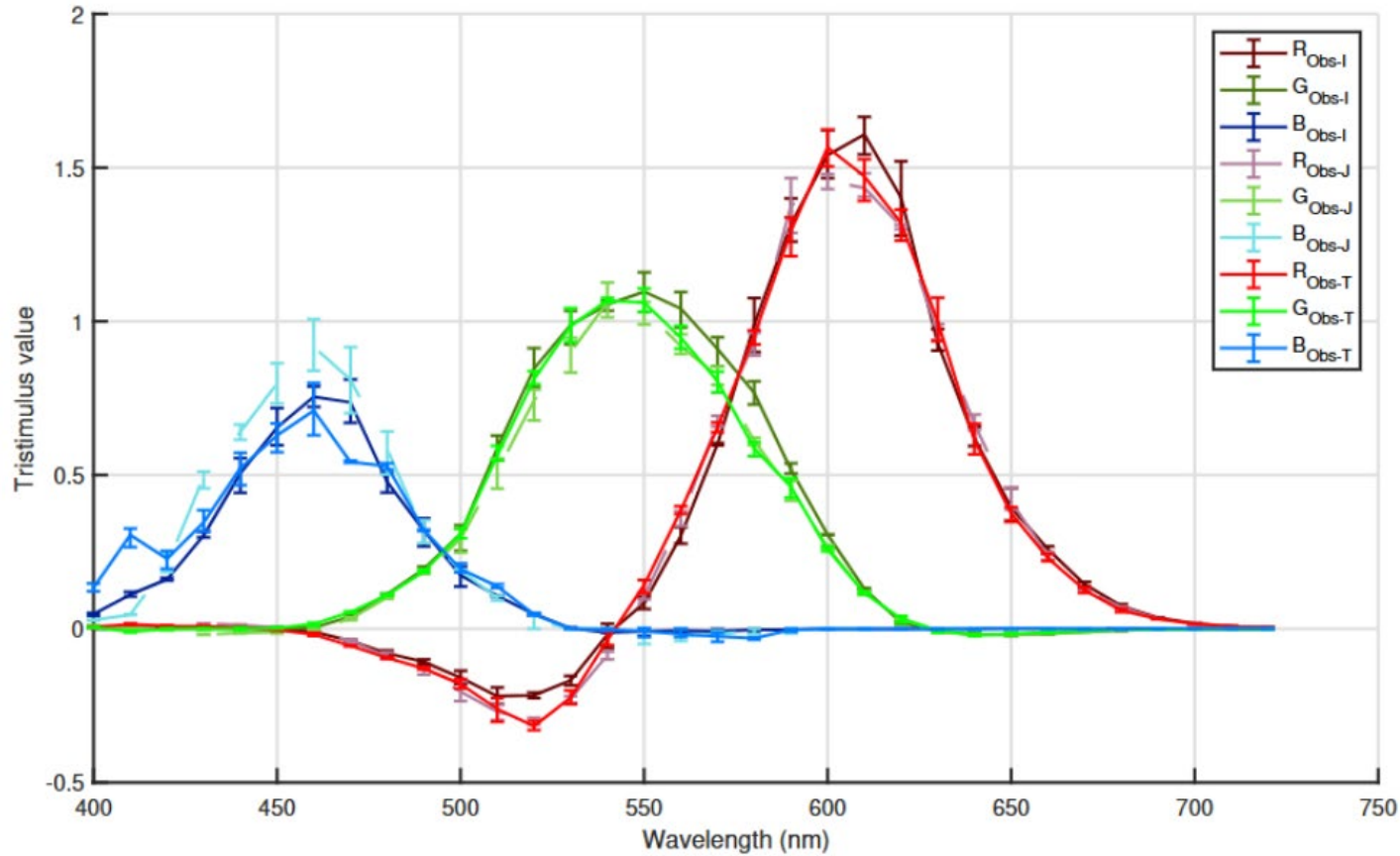


Fig. 11. Comparing the CMFs of three observers for inter-observer differences

Rago, Luvin, Ivar Farup, and Jan Henrik Wold. "Apparatus and Method for Measuring Individual Colour-Matching Functions." (2024).

Results

rg-chromaticity diagrams

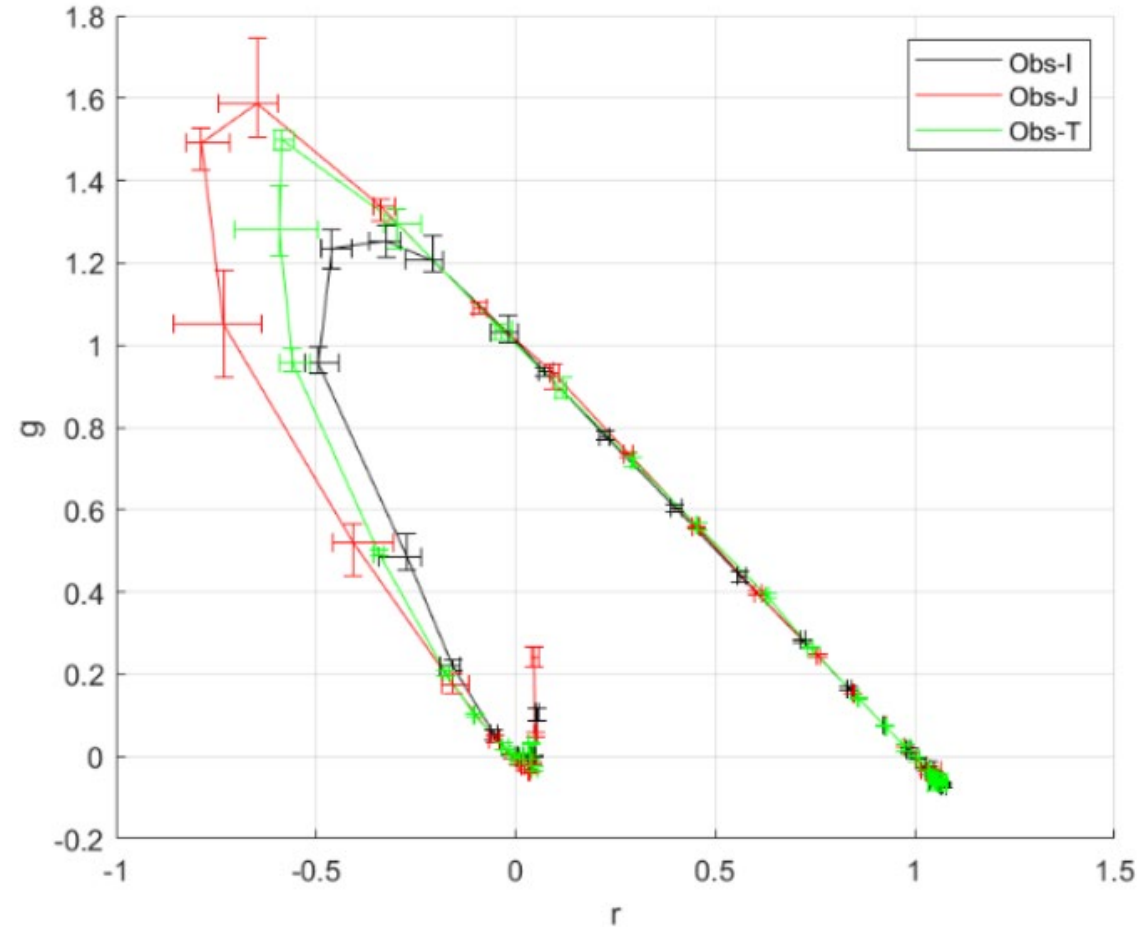


Fig. 12. rg-chromaticity diagrams with error bars of observer I, J and T.

Results

Colorimeter performance

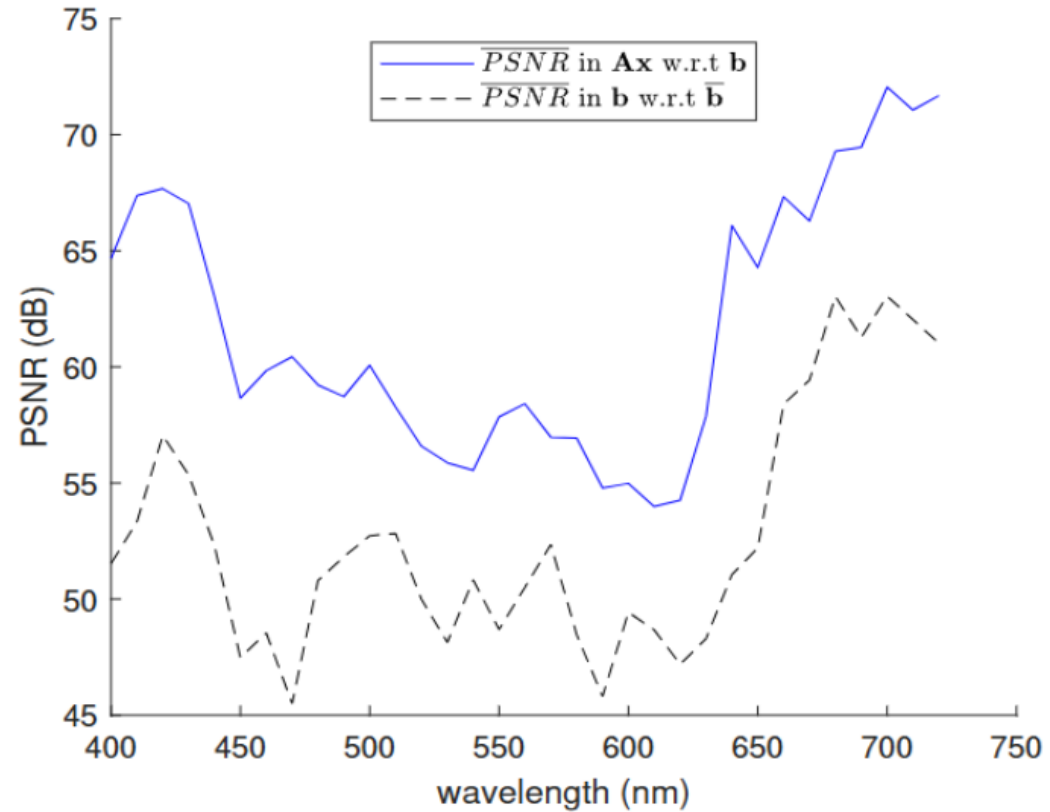
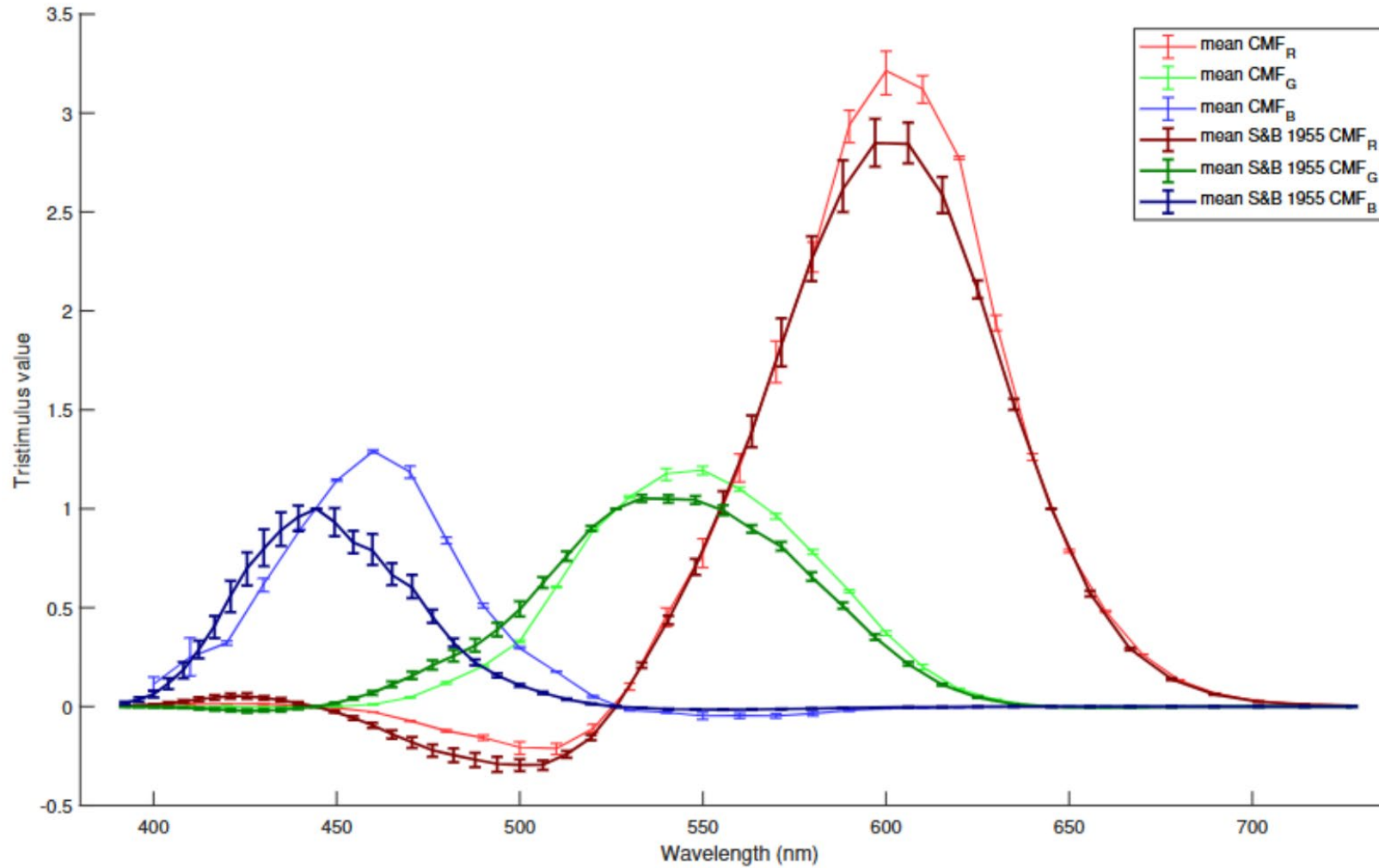


Fig. 13. Mean PSNR for all observers

Results

Comparing with mean Stiles and Burch 1955 CMFs





Colorimeter is simple, compact and relatively cheap.

It can measure intra- and inter-observer differences in individual CMFs with reasonable accuracy.

Further investigations required to investigate discrepancy with Stiles and Burch 1955 CMFs

Experiments are time-consuming.
Faster estimation methods need to be explored.



Apparatus and Method for Measuring Individual Colour-Matching Functions.

Ragoo, Luvín, Ivar Farup, and Jan Henrik Wold. (2024).
Optica Open. Preprint. <https://doi.org/10.1364/opticaopen.26235254.v2>